



CARTEMI 2004, Ischia

Application of Quasitopoi, Galois Connections, 16 years after ...



abstract

Application of Quasitopoi, Galois Connections, 16 years after ...



**Int'l Conference on Real Analysis and Measure Theory »CARTEMI«
Ischia, Italy, 2004**

"Application of Quasitopoi, Galois Connections, 16 years after ..."

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eM Institute, "located world wide" (L'Aquila, Hannover, Montpellier, Toledo, ...)

abstract:

For practical purposes it is really one of the most efficient ways to construct limits (and colimits) via simple liftings of limits (colimits) of atoms for the corresponding universal structure. Applying these techniques is nothing else than just practising the real kernel of Topoi, Galois Theory, and other universal constructions.

Lifting of Galois Connections is applying atoms in Galois Theory. We will give examples for industrial applications with regard to topological editors and topological navigation techniques, optimisers, pattern recognition, forecasters, chasing correspondences in data universes, data and referential integrity, and time series.

Working with "measures" means in this sense use of "continuous accumulations" instead of values for individual intervals, working "analytically" corresponds to universal principles, e.g. partial morphisms, cartesian closedness, limits and so on instead of methods from numerical analysis.

The "*spirit of topological structures in the sense of Alexander Grothendieck*" helps nowadays even with constructing models for theoretical physics as well as computer science.



agenda

Application of Quasitopoi, Galois Connections, 16 years after ...



- **C**ategorical background
- **A**toms for concrete constructions / algorithms
- **R**iemann goes Topology
- **T**opological universes
- **E**uler abstracts for applications
- **M**easure theory
- **I**ndustrial applications

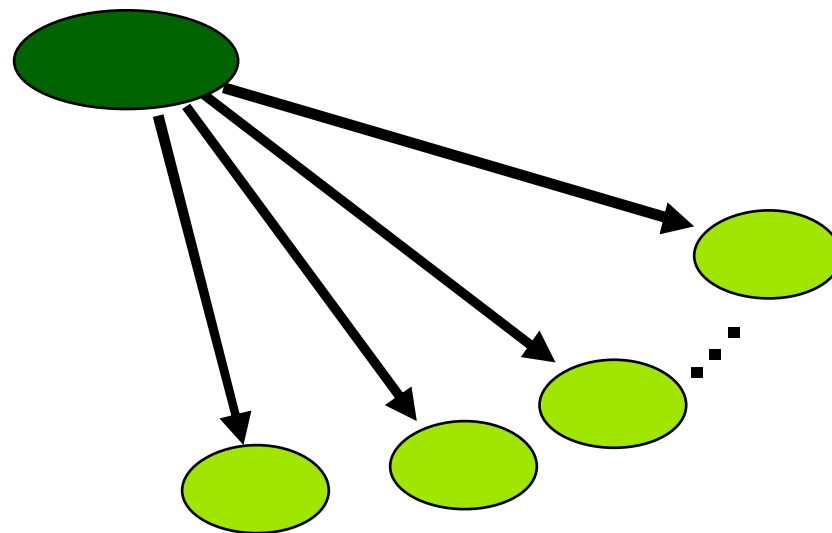


category topology

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top cats - initial structures
and the dual -
final structures



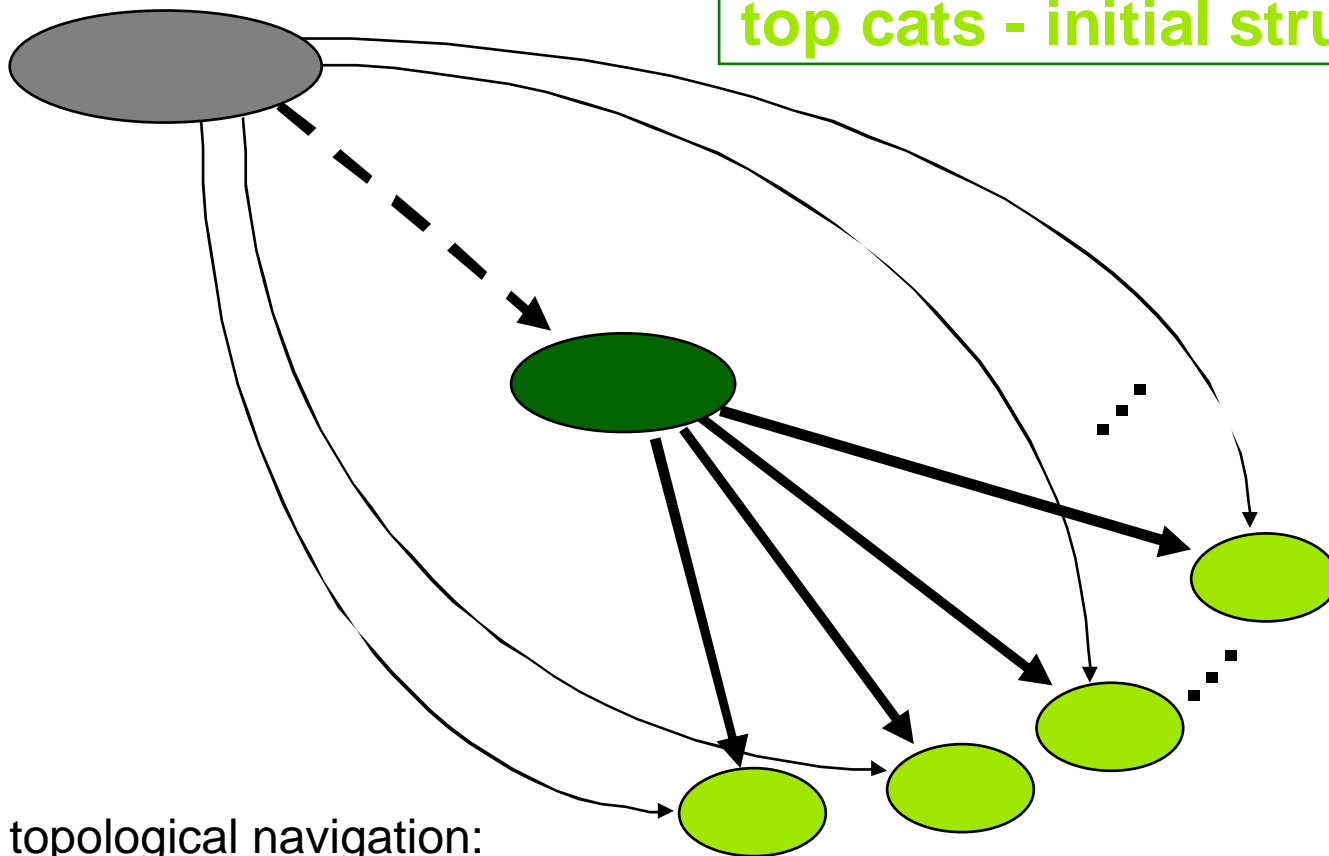


category topology

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top cats - initial structures



relevant for topological navigation:

subspace (easy handling, construction & views of parts of grids) **dual: quotient**

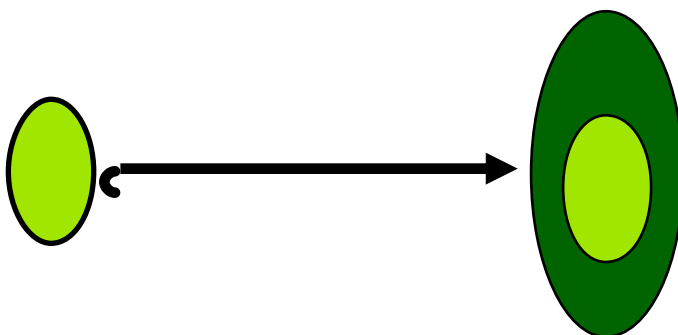
product (all different views easy to construct, navigate & linkable) **dual: coproduct**





quasitopoi partial morphisms

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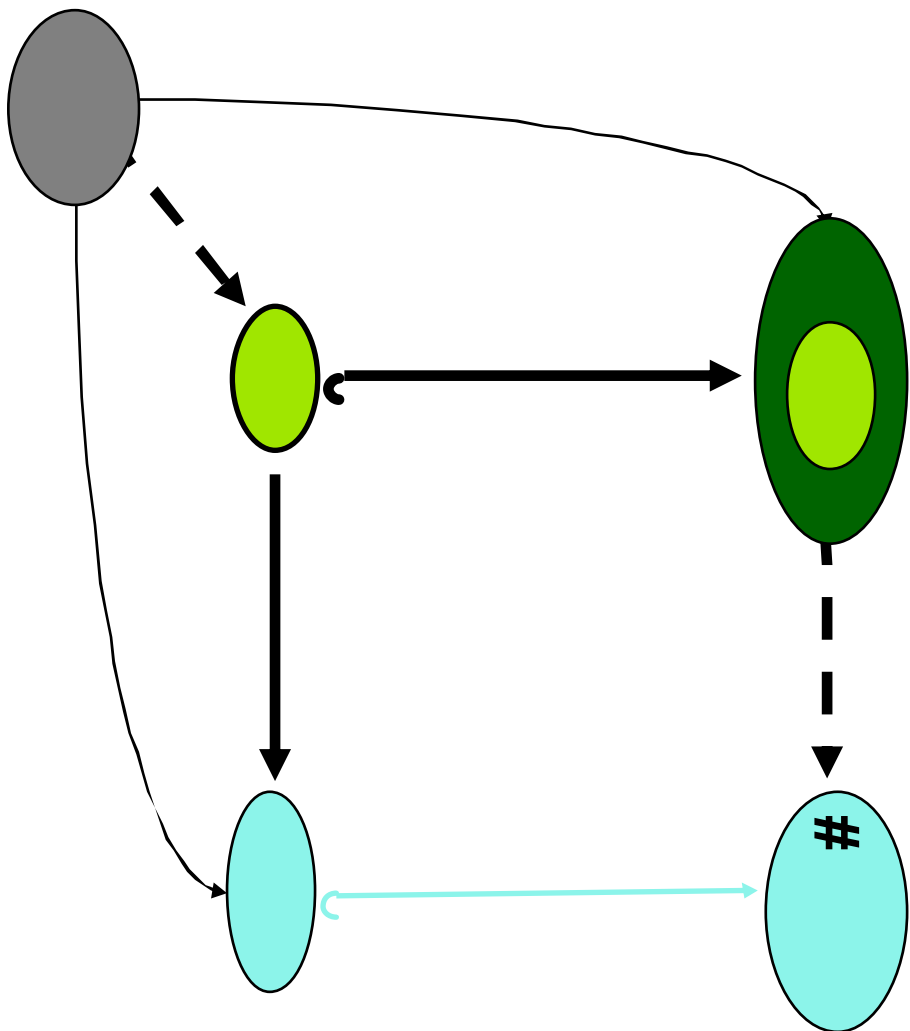


quasitopoi partial morphisms

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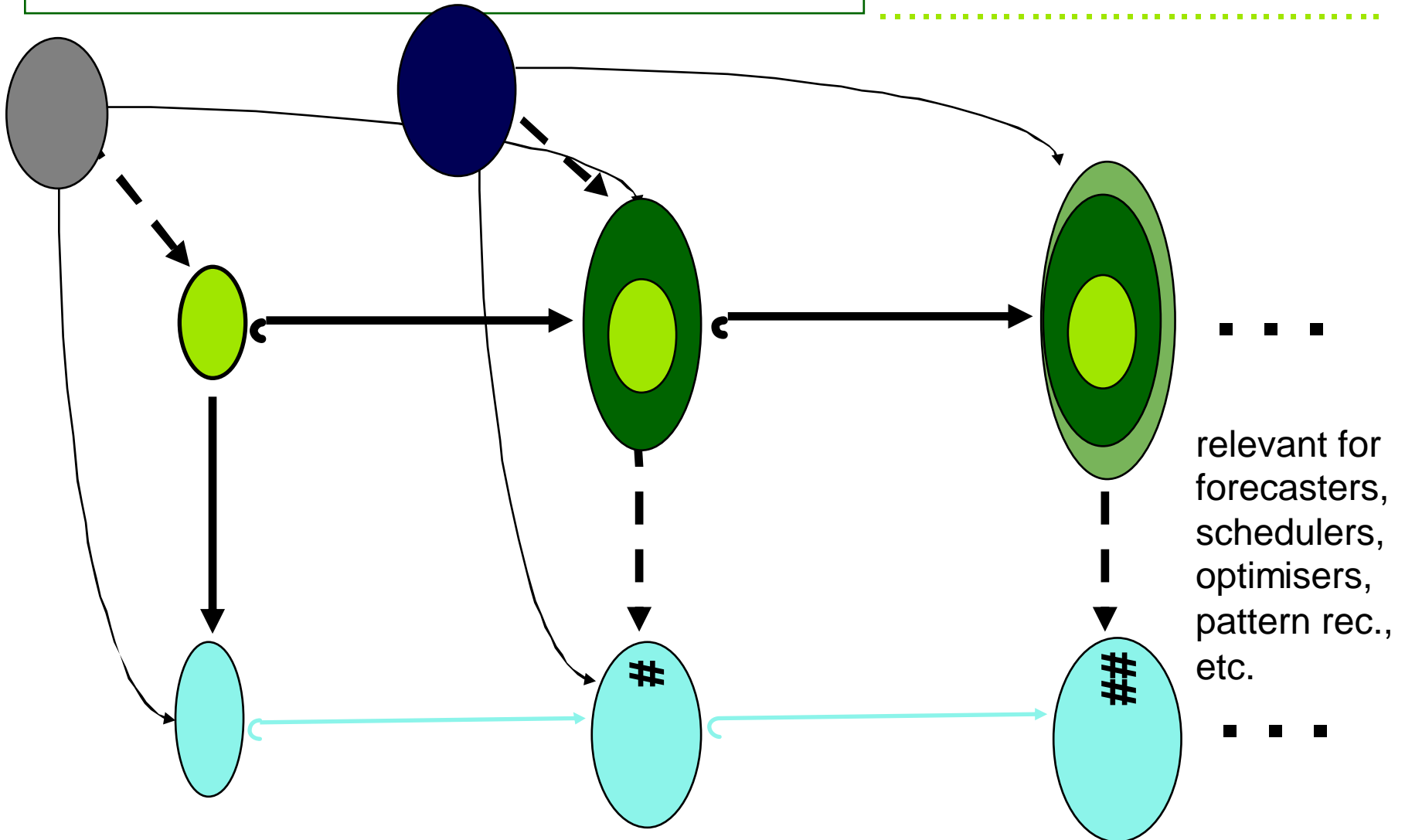
1-point-extensions ...





quasitopoi: partial morphisms

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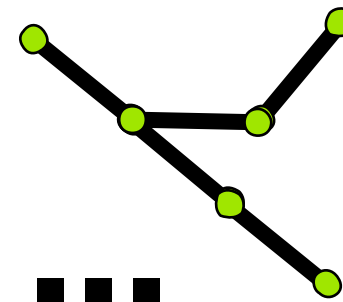
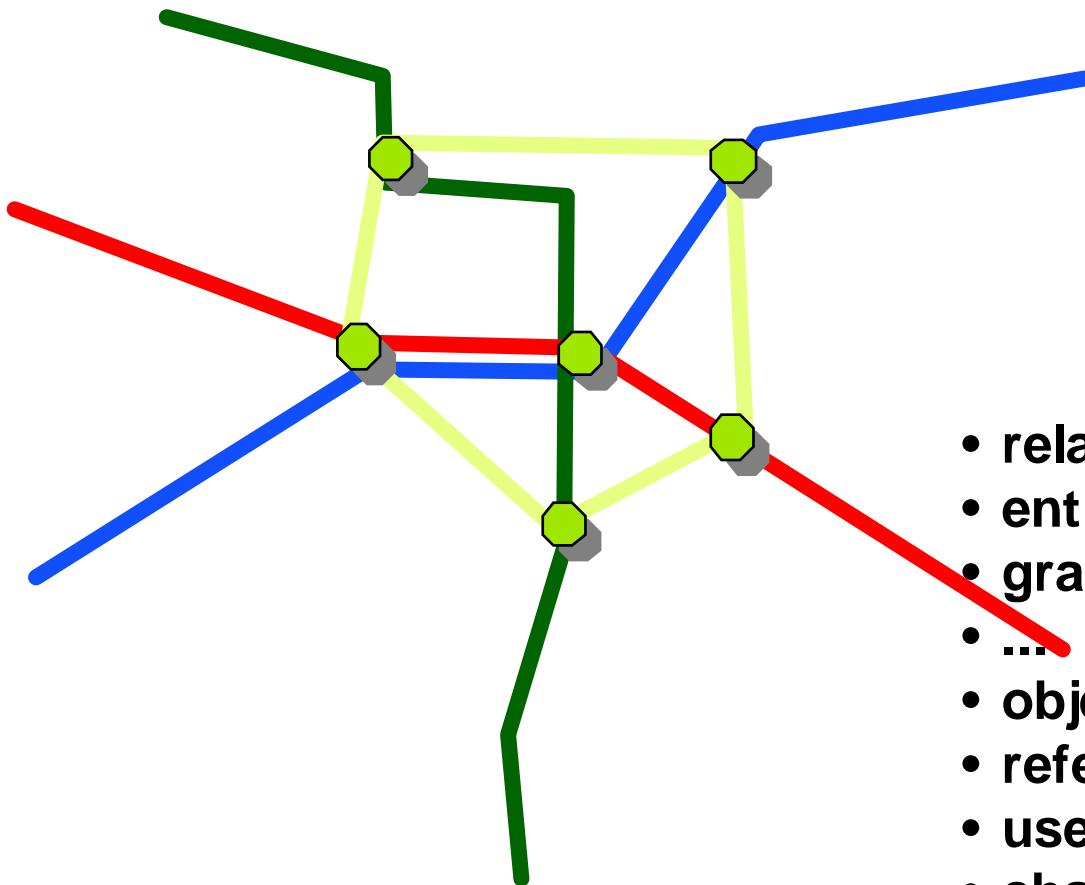


relevant for
forecasters,
schedulers,
optimisers,
pattern rec.,
etc.



relations vs points

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- relational DBs
 - entity relationship models
 - graph theory in comp. sc.
 - ...
 - object orientation (oop)
 - referential integrity
 - user's view
 - chaos in big info systems
- need of cat top assistance**





SCADA & ConCADA

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SCADA*):

- steering of physical grid
- control of infrastructure
- and other features

ConCADA**):

- GasPortfolioManagement
- steering of contracts
- control of contractual limits
- optimising flexibility
- and other features

*) **S**upervisory **C**ontrol **A**nd **D**ata **A**cquisition

***) **C**ontract **C**ontrol **A**nd **D**ata **A**cquisition

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where we have to go ... ?

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my 5-point-"edit"-program: computer assistance for

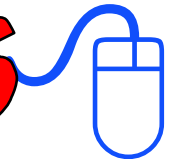
- ≅ better isos e.g. automation for order number for visualisation, ...
- 👁 part of grid (subspaces)
- 📱 gluing together grids (coproducts)
- ❄ simplifying grids/interrelations, "portfolios" (quotients)
- 👤 product of grids (products)

cattop editors

my 5-point-"navigator"-program: computer assistance for

- ≅ "topology" of configuration (ref. integrity)
- 👁 arbitrary relation (or point/object) "on top" (e.g. not)
- 📱 neighbourhoods stepwise visible (partial homeomorphisms)
- ❄ alternative info ("fuzzy", "names")
- 👤 "pattern" recognition/quick construction/reuse of path

+ cattop navigators



=> new topological features required !!!





A.G.'s Galois Theory

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Galois Theory

- universal constructions

atoms for construction of

- limits

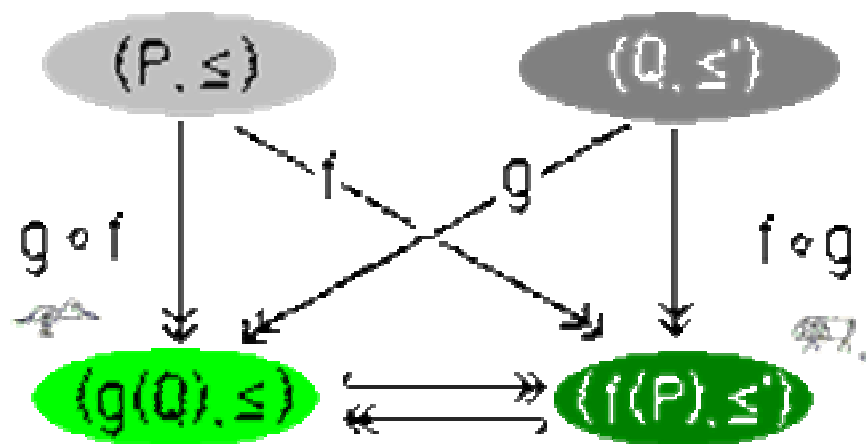
and the dual

- colimits

=>

lifting of Galois Connections

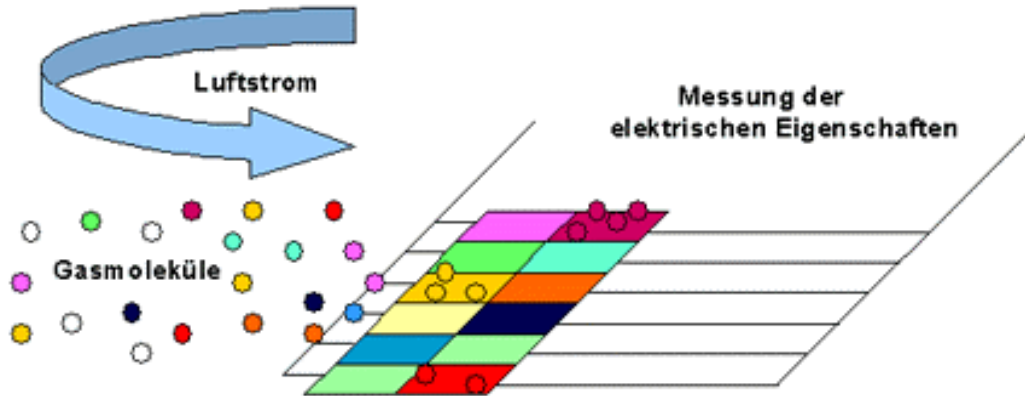
atoms in Galois Theory



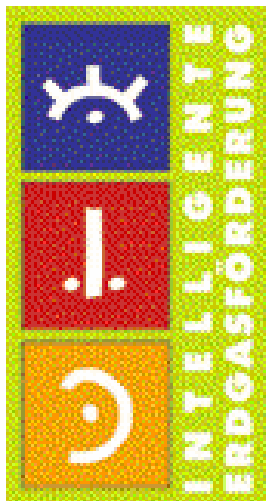


Human Interface Supervision System

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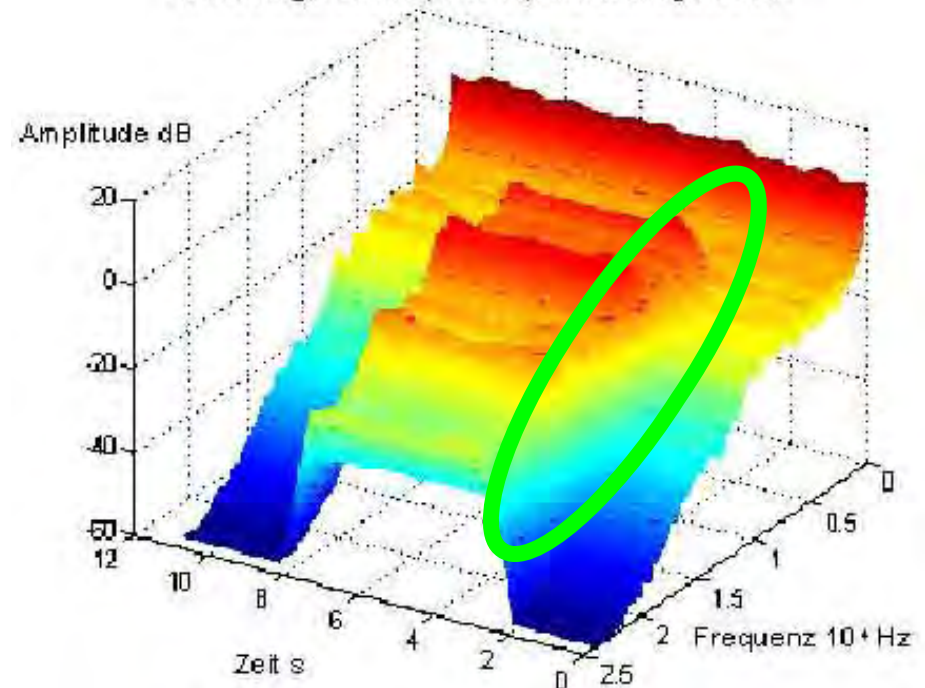


Dotierte Trägerplättchen



**pattern recognition:
fuzzy logic & neural nets
better => PreTOPs**

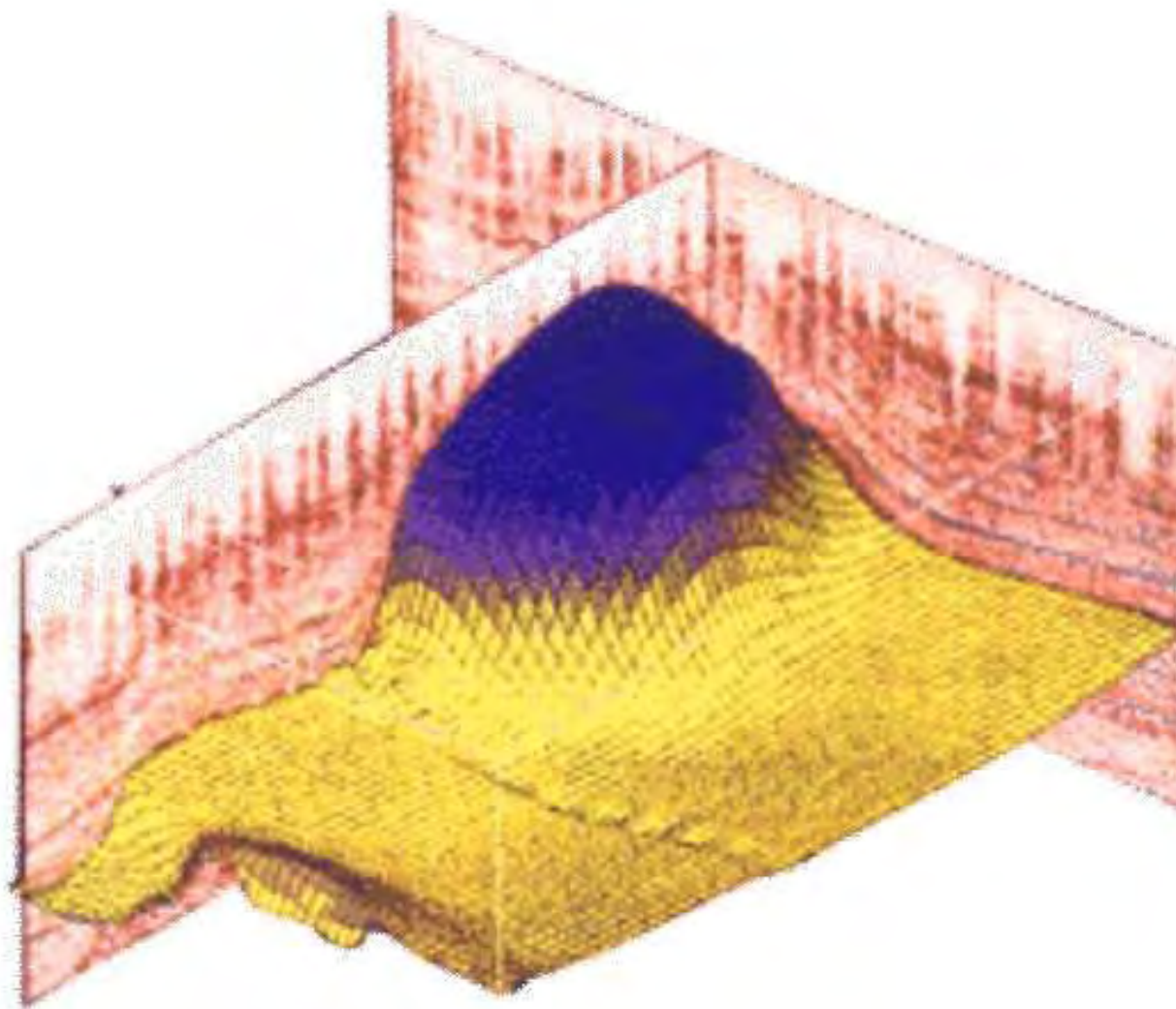
Ausströmgeräusch (5Nm³/h) mit Grundgeräusch





industrial applications

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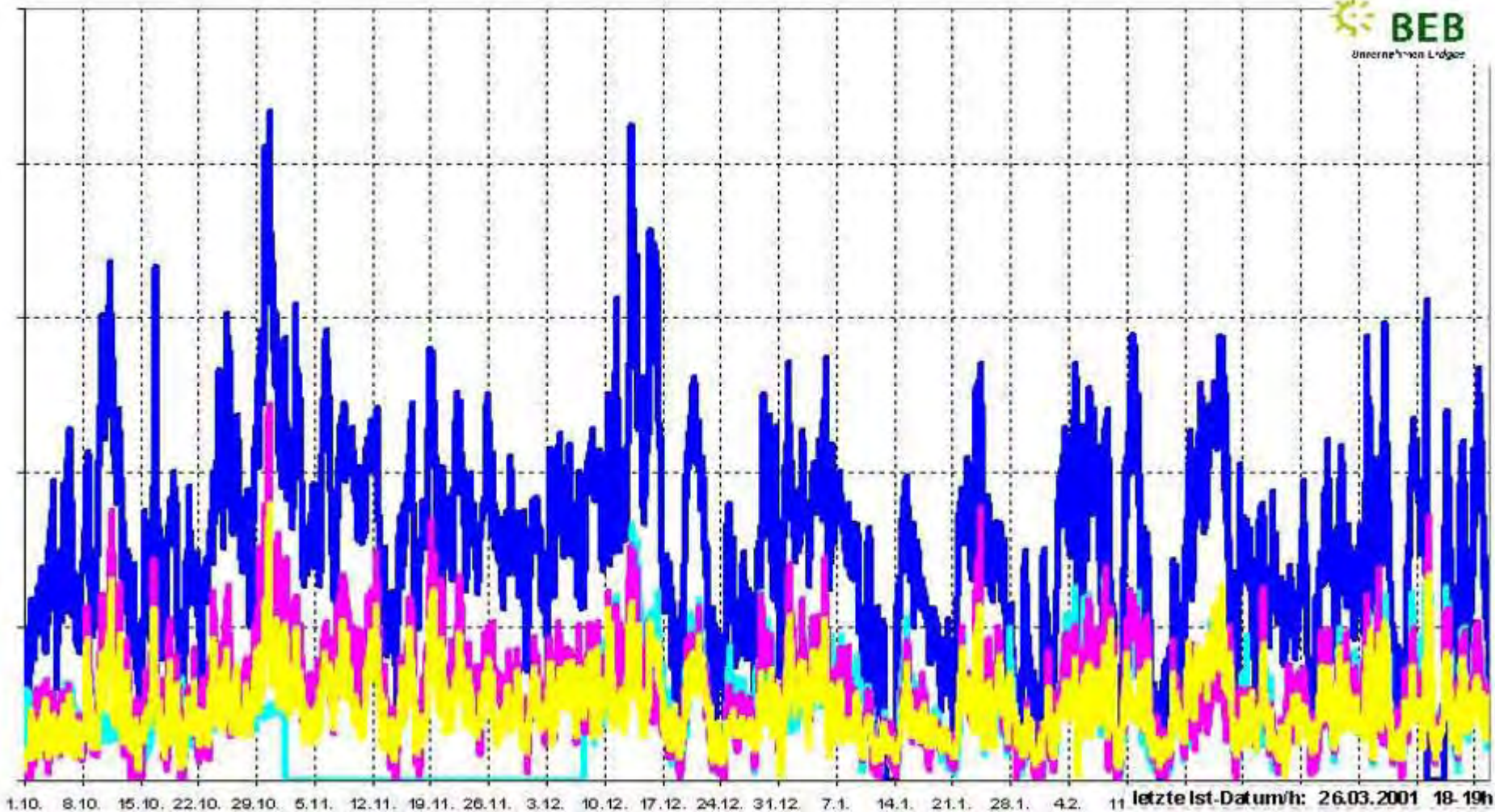
relevant for forecasters, schedulers, simulators, optimisers, pattern rec., etc.





time series

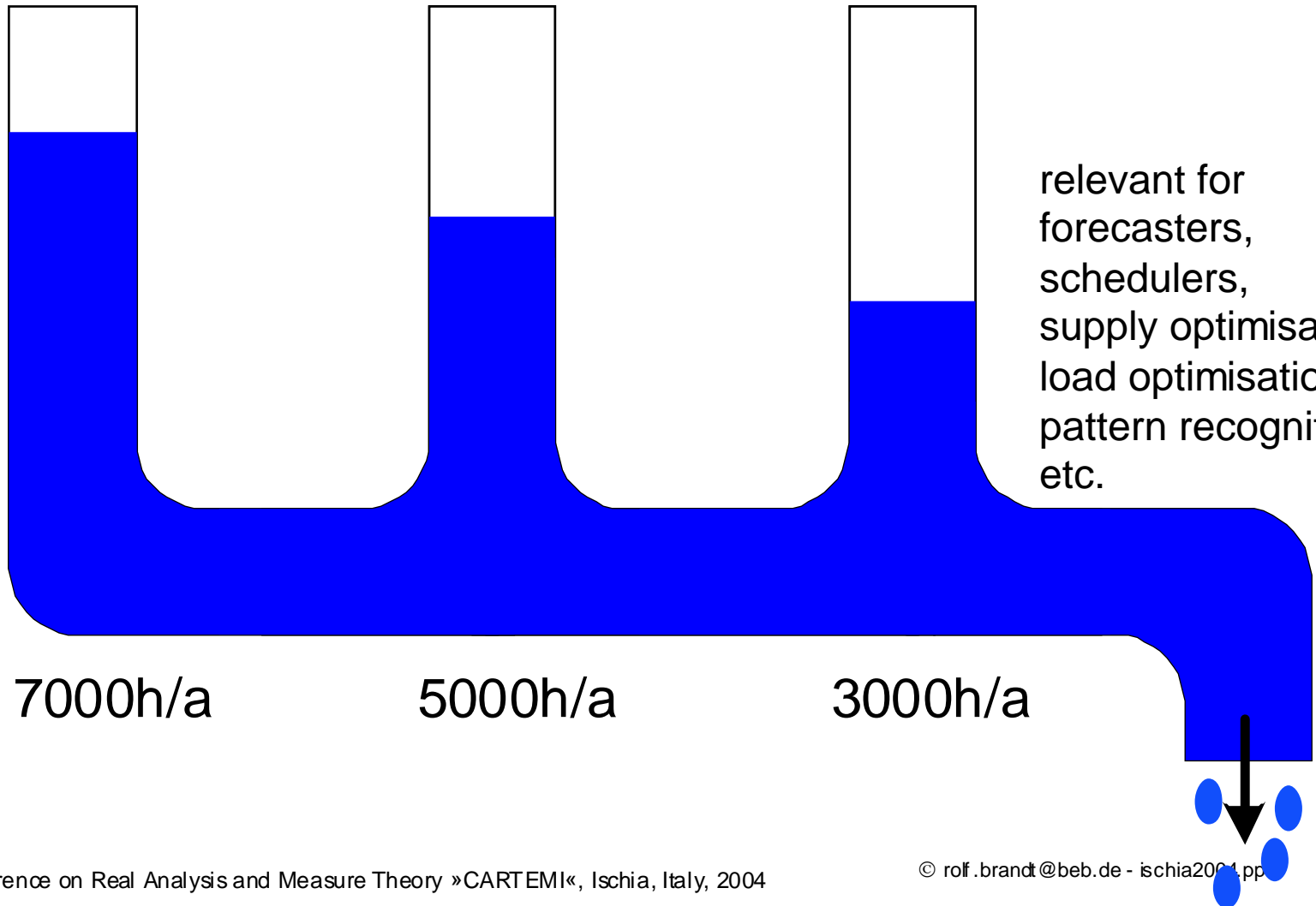
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bin packing

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forecasters

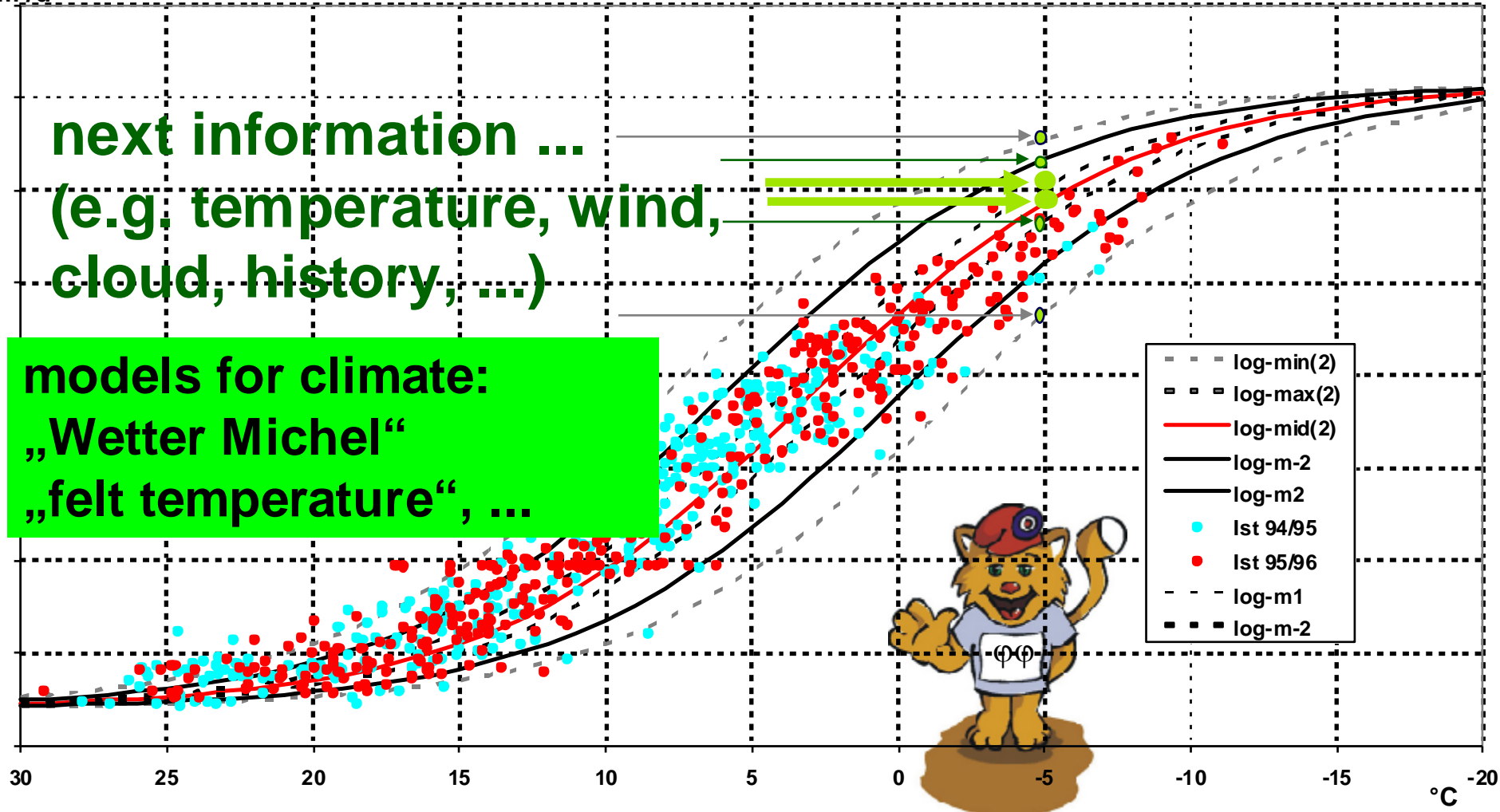
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m³/d

next information ...
(e.g. temperature, wind,
cloud, history, ...)

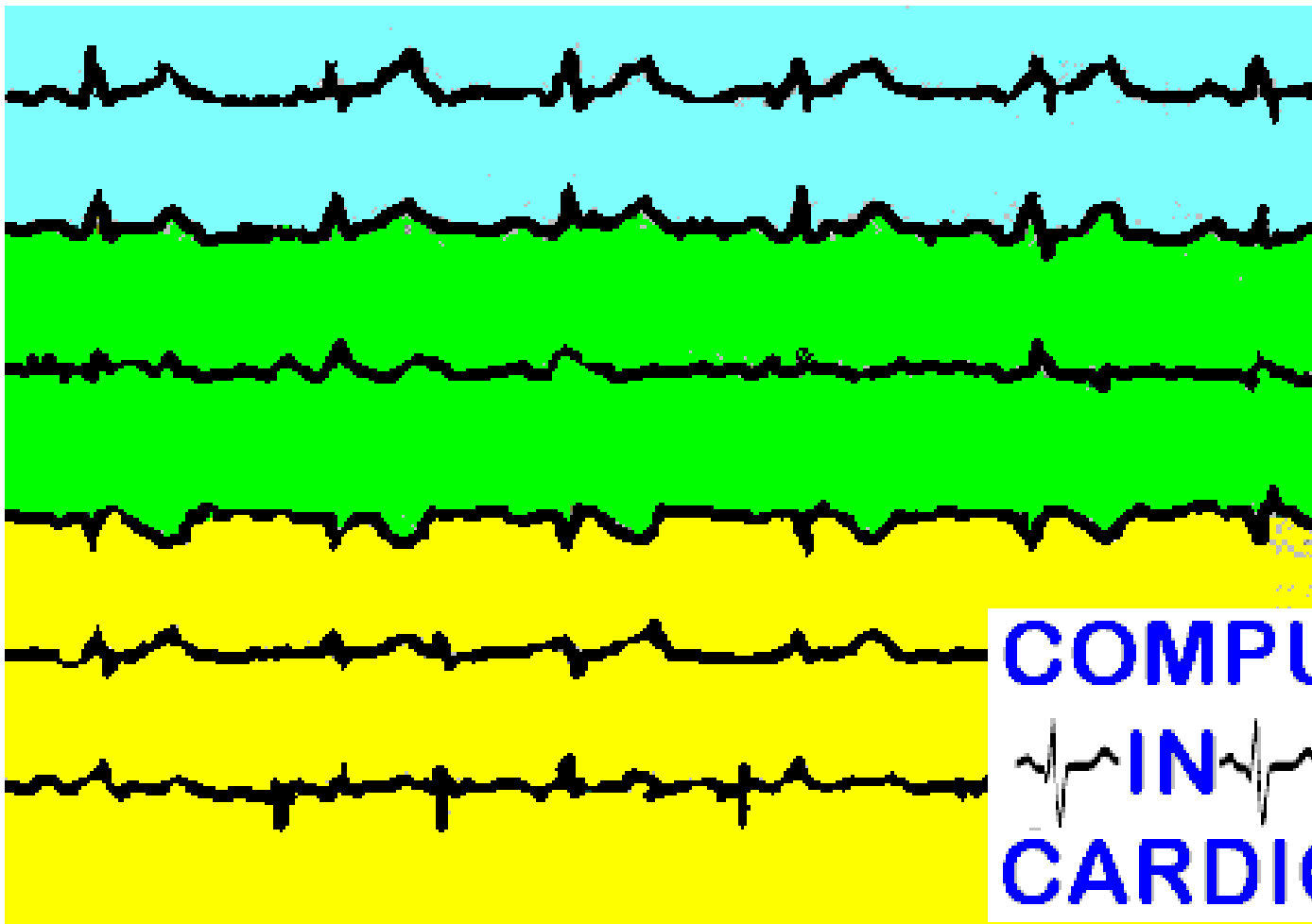
models for climate:
„Wetter Michel“
„felt temperature“, ...





ECG's

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... thank you
for your
kind
attention ...

